$\operatorname{COMPCERT}$: C compilers you can formally trust

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Overview of $\operatorname{COMPCERT}$ Implementation

Bug trackers of GCC and LLVM (Sun-et-al@PLDI'16)



The number of attested bugs tends to remain almost constant. New bugs are introduced when compilers are improved !

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 \neq "performance" bug in an optimization.

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Optimizing compilers are quite large software (in MLoC) with hundreds of maintainers, e.g : https://github.com/gcc-mirror/gcc/blob/master/MAINTAINERS

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Another fundamental reason :

Tests of *optimizing compilers* cannot cover all corner cases because of a combinatorial explosion.

Strong safety-critical requirements of

DO-178 (Avionics), ISO-26262 (Automotive), IEC-62279 (Railway), IEC-61513 (Nuclear) often established at the source level...

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Better solution a *formally proved* compiler for formal tool qualification (DO-178C + DO-333)...



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⇒ up-to-date & very sharp (formal) documentation of the compiler that may also help "*external developers*"

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Part of an ongoing effort to certify a whole software chain in the $\rm Coq$ proof assistant

from the prover (e.g. CertiCoq) to OS kernels (e.g. CertiKOS) Example http://deepspec.org (supported by NSF).



Certifying compilers

The $\mathrm{Coq}\xspace$ proof assistant for certifying compilers

Using COMPCERT

Overview of $\operatorname{COMPCERT}$ Implementation

The Coq proof assistant for certifying compilers

The $\mathrm{COQ}\xspace$ proof assistant

A *language* to **formalize mathematical theories** (and their proofs) **with a computer**. Examples :

- Four-color & Odd-order theorems by Gonthier-et-al.
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- Logic reduced to a few powerful constructs; Proofs checked by a small verifiable *kernel*
- Consistency-by-construction of most user theories (promotes *definitions* instead of *axioms*)

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Results from a long history in formalizing mathematical reasonning since Frege, Russel, Hilbert near 1900.

Formally proved programs in the COQ proof assistant

The ${\rm Coq}$ logic includes a functional programming language with pattern-matching on tree-like data-structures.

Extraction of COQ functions to OCAML + OCAML compilation to produce native code.

 \Rightarrow CompCert is programmed in both Coq and OCaml.

- A typed programming language, only handling data of the form
- inductive data (tree-like data)
- (pure) functions (with structural recursion)
- types, where $Type_i$ is the type of $Type_j$ with j < i

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Example where z in $Type_0$ is the type of relative integers

```
Inductive nat: Type := 0 | S(n:nat). (* defines natural numbers *)
Fixpoint plus (n m:nat): nat := (* defines n+m recursively *)
match n with 0 => m | (S n') => (S (plus n' m)) end.
(* Type of tuples containing (S n) values in Z *)
Fixpoint tuple_S (n:nat): Type :=
match n with 0 => Z | S n' => Z * (tuple_S n') end.
(* Concatenation operation of such tuples *)
Fixpoint app (n m:nat):(tuple_S n)->((tuple_S m)->(tuple_S (S (plus n m)))) :=
match n with
0 => fun t1 t2 => (t1, t2)
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Decidable typechecking with *computations in types* ! Only *structural* recursion is allowed \Rightarrow all computations terminates.

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Typing rule : when A: Type (with restrictions) and $P: A \rightarrow Type_i$ then forall (x:A), (P x) in Type_i

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Gives a *subset* of classical logic called *intuitionistic logic*. Classical logic recovered with a few additional axioms like

Axiom excluded_middle: forall (A:Prop), A \/ (A -> False).

A flavour of certifying compilers in COQ

COMPCERT proof is huge (> 100Kloc of COQ).

Follow this link to have a simpler example : http://www-verimag.imag.fr/~boulme/IntroCompCert/DemoCoq/



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Unequaled level of trust for industrial-scaling compilers Correctness proved within the COQ proof assistant

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Performance of generated code (for PowerPC and ARM)

 $2\times$ faster than gcc -OO 10% slower than gcc -O1 and 20% than gcc -O3.

In MTU systems (German provider of Nuclear Power Plants) 28% *smaller* WCET than with a previous *unverified* compiler.

Understanding the formal correctness of COMPCERT

Formally, correctness of compiled code is ensured modulo

- correctness of C formal semantics in Coq correctness of assembly formal semantics in Coq absence of undefined behavior in the source program

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Formal semantics \simeq relation between "programs" and "behaviors"

i.e. a (possibly non-deterministic) interpretation of programs

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- \bullet correctness of assembly formal semantics in Coq
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Source program assumed to be without undefined behavior

```
int x, t[10], y;
...
if (...) {
  t[10]=1; // undefined behavior: out of bounds
  // the compiler could write in x or y,
  // or prune the branch as dead-code, ...
```

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NB : under these conditions, C has no UNDEFINED-BEHAVIOR. Using COMPCERT

Trust in ELF binaries produced with $\operatorname{COMPCERT}$

Trust in binaries requires additional verifications, at least :

- ▶ absence of undefined behavior in C code (e.g. with ASTRÉE)
- correctness of assembling/linking (e.g. with VALEX)

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Qualification of MTU *development chain* for Nuclear safety from Käster, Barrho et al @ERTS'18

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COMPCERT's model of Intermediate Representations

Definition The transition semantics (of a program) is defined – on a given type of states – by :

- a subset of initial states (i.e. at "main" entry-point);
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- 4 kind of behaviors recovered by :
 - infinite sequence with a finite or infinite trace
 - finite sequence ended on a final state
 - finite sequence ended on a non-final state (*stuck*)
 ⇒ UNDEFINED-BEHAVIOR

Certifying compilation passes in COMPCERT

Theorem : correctness of forward simulations

The correctness of a pass between a source semantics on S_1 to a deterministic target semantics on S_2 , can be proved by a simulation relation $S_1 \sim S_2$ that :

- is established on initial states
- preserves final states
- and execution steps with :



NB : condition $|{\it S}_1'|<|{\it S}_1|$ ensures preservation of infinite silent loops.

Untrusted Oracles in COMPCERT

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Benefits of untrusted oracles

simplicity + efficiency + modularity

Modular design of COMPCERT in COQ

Components independent/parametrized/specific w.r.t. the target



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Demo on a mini example for x86-64 target at this link :

http://www-verimag.imag.fr/~boulme/IntroCompCert/DemoCompCert/